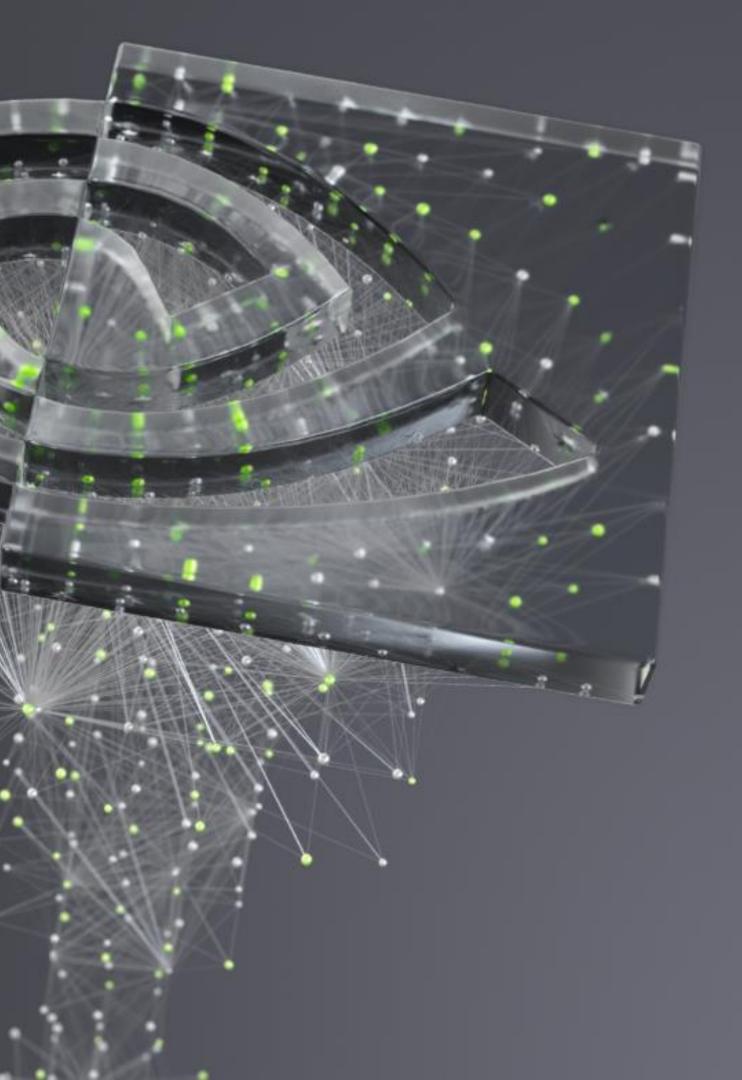


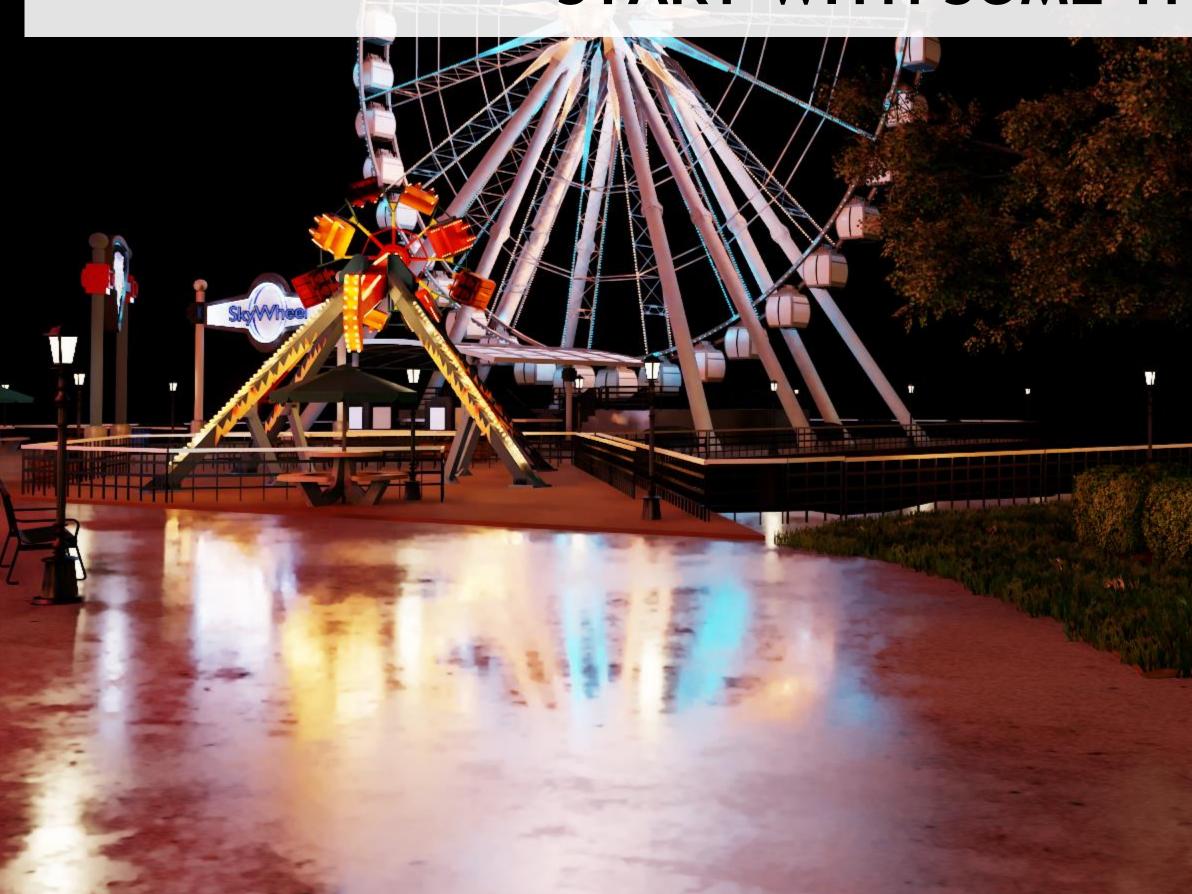
REFRAMING LIGHT TRANSPORT FOR REAL-TIME

Chris Wyman Principal Research Scientist

High Performance Graphics 2020



START WITH SOME THANKS



Real-time capture, 3.4 million area lights

START WITH SOME THANKS A lot of the thoughts you'll hear were informed & helped along by numerous others

Benedikt Bitterli,

Wojciech Jarosz, Matt Pharr, Peter Shirley, Aaron Lefohn,

Kate Anderson,

Alexey Panteleev, Tim Cheblokov, Pawel Kozlowski, Jacob Munkberg, Jon Hasselgren, Mike Songy, Petrik Clarberg, Simon Kallweit, Marco Salvi, William Newhall, Bob Alfieri, Jacopo Pantaleoni, John Burgess, Apollo Ellis, Kai-Hwa Yao, Lucy Chen



Real-time capture, 83,000 area lights

Real-time ray tracing is here!

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Big question... What's it good for? Besides the obvious:

Offline: Accelerate computation

Real-time: Better shadows, AO, reflections

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Real-time ray tracing is here! Big question... What's it good for? Besides the obvious: Offline: Accelerate computation Real-time: Better shadows, AO, reflections Move to path tracing was good for film But we can't rely on Moore's Law for real-time performance Lots of space between "faster offline" & "better shadows" Few have applied constraints of real-time rendering to general problems in ray and path tracing



Real-time capture, 13,000 area lights + emissive environment map

Compute until time constraint reached (not a quality target)

Time-to-image is a key metric; include per-frame data structure build costs

Desire tunable quality knobs

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Assume scenes are dynamic

And we want robustness even under user control

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Spatial and temporal reuse assumed

Either to reduce cost or increase quality at a given cost

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Managing data and code divergence and incoherence

THERE'S BEAUTY & ELEGANCE IN BRUTE FORCE But care is required for real-time



Real-time capture, 7,500 area lights + emissive environment map

THERE'S BEAUTY & ELEGANCE IN BRUTE FORCE But care is required for real-time

Simply not possible for many problems

E.g., can't expect to touch millions of lights, for all pixels, for all frames

E.g., can't trace all subsurface scattering paths

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Suggests we need for stochastic techniques

But must work in a streaming fashion, to fully leverage GPU resources

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Integrates a non-analytic (and unknown) function

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Light BVH

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Look for help from... political polling

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Never know the collective ground truth, and it can change day-to-day Actual voting (i.e., the ground-truth sensor) depends on who shows up Uses only a few hundreds to thousands of samples; these take days to weeks to collect Frequently cannot choose samples; must correct for the distribution you get Quite accurate, considering they prefilter *prior* to a binary decision

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Particularly interesting aspects include:

Spatial and temporal aggregation often improves predictive quality

DON'T TRUST POLITICAL POLLING?

Numerous other applications:

Over 100 US agencies collate statistics

Census, employment, economic indicators, resources, infrastructure, etc., etc.

Most with error **much** lower than 3-5%

With more expensive and principled sampling, regularly validated with measurements

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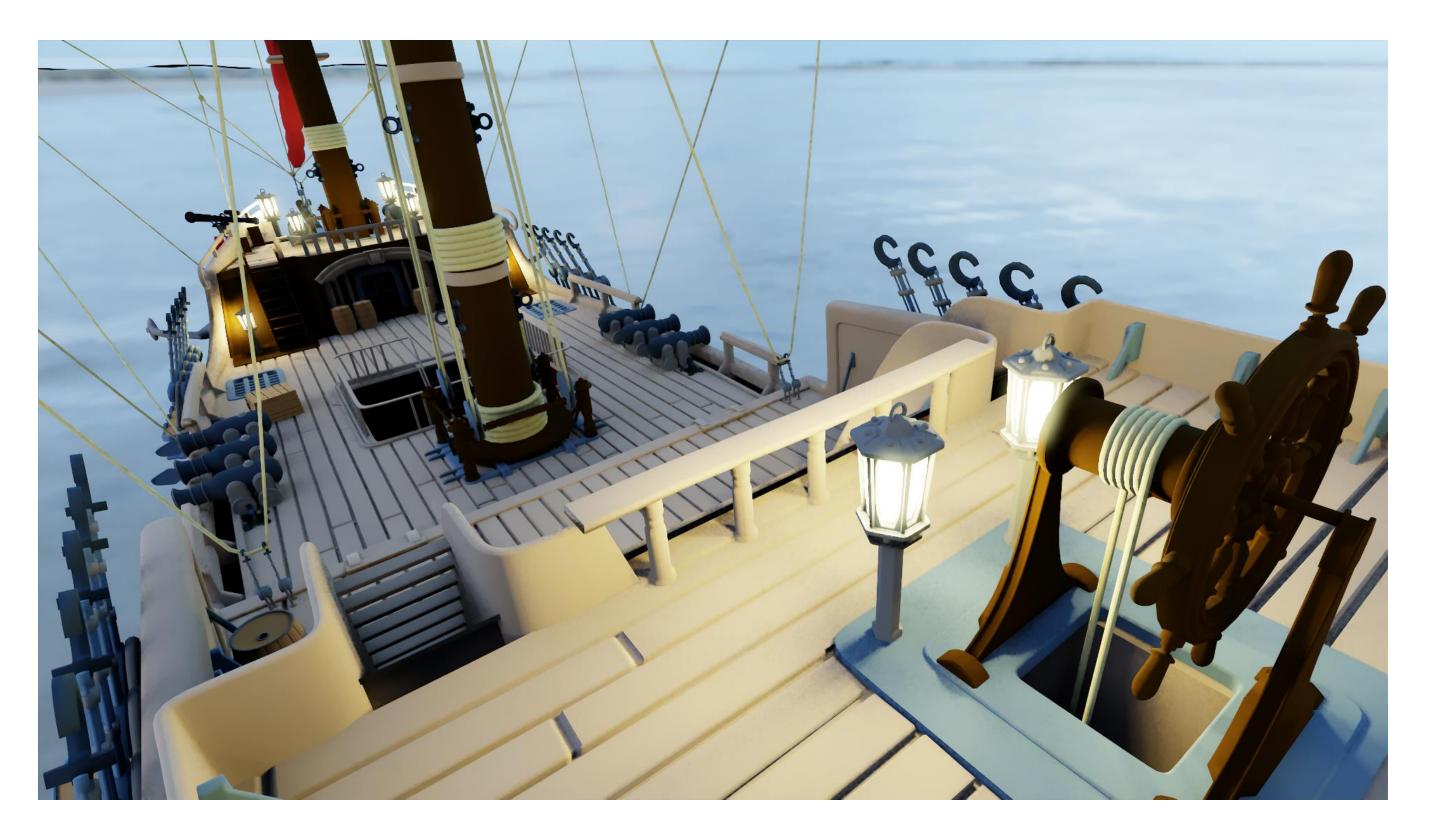
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Particular call out to <u>Statistics Sweden</u>:

Open-access, peer-reviewed "Journal of Official Statistics"

Many of their statisticians write supremely clear articles that I found invaluable



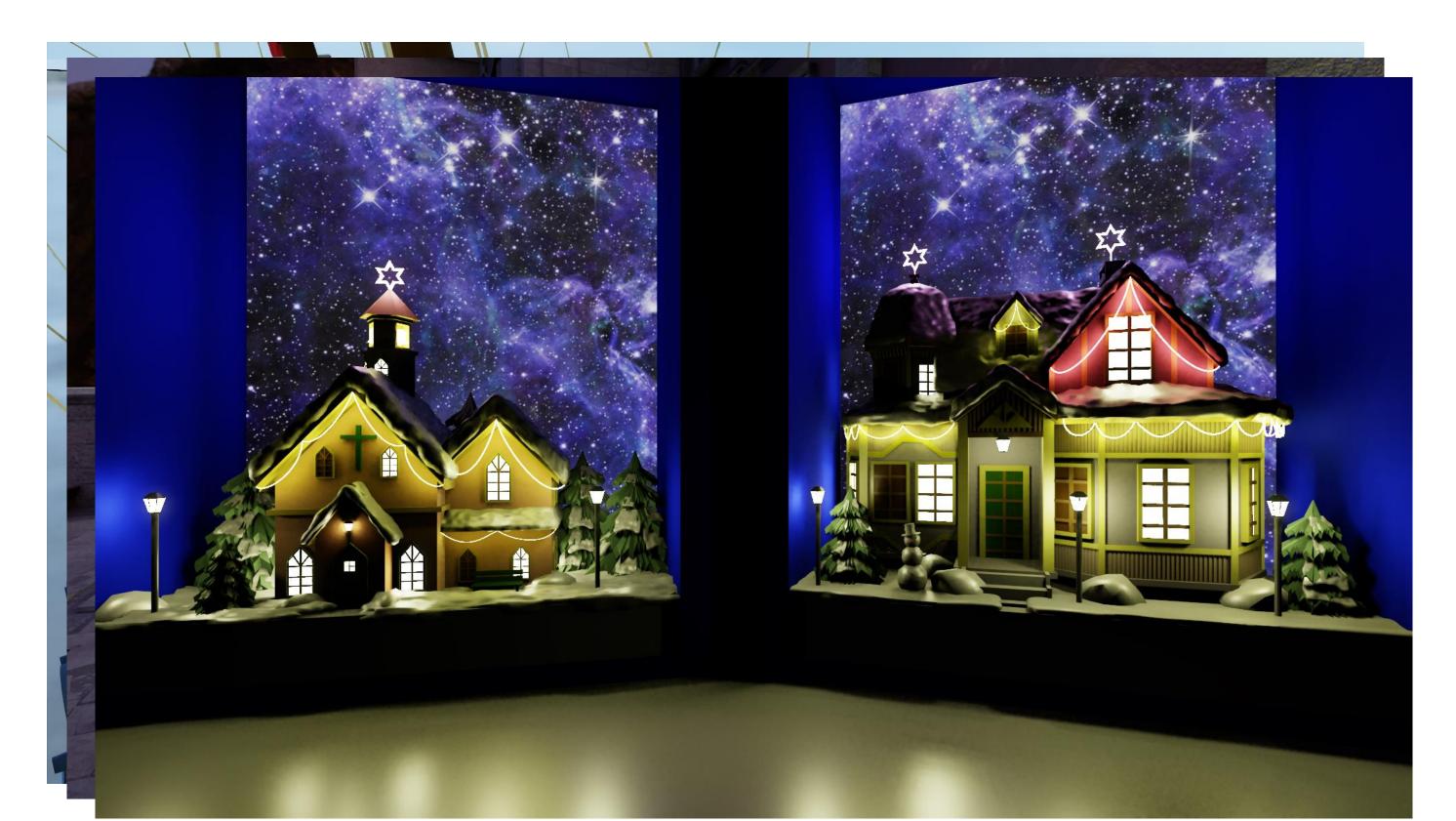
5 minutes from unlit model to this

Suzanne's Revenge from Blend Swap (user gregzaal)



A tired 8+ year old asset gains new life

Tagged two matl's as emissive & added environment map



Asset I pulled from BlendSwap

(from user Mikel007)

Hardest part: converting model format to load

CONSIDER REAL-TIME RENDERING TODAY What do people do when they have insufficient resources?



Real-time capture, 1100 area lights + emissive environment map

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Accumulation buffering / progressive rendering

(Ir)radiance caching / light probes

Antialiasing techniques

Denoising and reconstruction filters

Adaptive sampling

... and probably many more

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... and probably many more

Also common in more offline contexts

E.g., path guiding, radiosity, etc.

Pixel colors

Texture colors

Colors (in other spaces)

Antialiasing, post-process filtering, (typically) denoising filters Light maps, environment maps Irradiance volumes

Pixel colors	Antialiasing, post-process filtering, (ty
Texture colors	Light maps, environment maps
Colors (in other spaces)	Irradiance volumes

During reuse, lost most non-color information Easy to blur visibility Easy to blur specular highlights Easy to add bias

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Projected radiance

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Colors (in other spaces)	Irradiance volumes
Projected radiance	Spherical harmonic coefficients

cypically) denoising filters

More expensive to (pre-)compute Reduces problems reusing color But not fully eliminated

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Visibility

Antialiasing, post-process filtering, (typically) denoising filters Light maps, environment maps Irradiance volumes Spherical harmonic coefficients Shadow maps, form factors, ambient occlusion

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Projected radiance	Spherical harmonic coefficients
Visibility	Shadow maps, form factors, ambient of

cypically) denoising filters

occlusion

Visibility (mostly) always binary Reuse = filtering Hard *not* to blur or alias

Pixel colors Texture colors Colors (in other spaces) Projected radiance Visibility Ray segments

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Ray segments	Bidirectional path tracing, light field r
Probabilities	Adaptive ray tracing, path guiding
Random variates	Primary sample space techniques

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rendering

Less well explored in real-time Handles issues from above reuse Big question: Efficient algorithms?

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Usually for "smooth", "small", or just "understandable" changes

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Blurring, aliasing, lag, ghosting, halos, ringing

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Assertion: Artifacts less correctable later in the rendering process Postprocessing final colors? Lost most data needed to correct for broken assumptions

Why?

Importance sampling function can be nearly arbitrary

If well chosen, convergence improves significantly

If poorly chosen, worst case added noise

Rationale:

Good reuse, where assumptions hold, improves in quality significantly A few places pixels become noisier, when reuse assumptions fail

- (!/\$ increase)
- (!/\$ decrease)

Consider this reuse assumption:

Nearby pixels have similar probability to select a given light sample (or path vertex)

(Can probably replace "pixel" with "texel" or "voxel")

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What does that even mean?

If you construct a per-pixel sampling PDF, "aggregate" them to improve quality?

Importance sampled Monte Carlo integration:

 $\int f(x) \, dx \approx \frac{1}{N} \sum \frac{f(x_i)}{p(x_i)}$

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Idea: Target perfect importance sampling, $p(x) \propto f(x)$? Reduces samples needed to one But when importance sampling is taught, the idea is handwaved away

WHAT DOES PERFECT IMPORTANCE SAMPLING MEAN? And should we really ignore it out of hand?

If $p(x) \propto f(x)$, this means p(x) = cf(x) for some normalization constant

Since for any PDF, $\int p(x) dx \equiv 1$, it's easy to show $c = \frac{1}{\int \int f(x) dx}$

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But... If we're using Monte Carlo integration, why would an integral bother us? We're already approximating, so can we just apply more Monte Carlo?

Imagine you have unnormalized $\hat{p}(x)$ you want to use for importance sampling

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 using a Monte Car

Plug p(x) back into the original Monte Carlo estimator and you get:

$$\int f(x) \, dx \approx \frac{1}{N} \sum \left[\frac{f(x_i)}{\hat{p}(x_i)} \, \frac{1}{M} \sum \frac{\hat{p}(x_j)}{q(x_j)} \right]$$

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This is exactly the RIS estimator See Talbot et al., EGSR 2005

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Take M samples from distribution q(x), turn into N samples from (unnormalized) distribution $\hat{p}(x)$

(cheap, low-quality, or simply bad)



(complex, high-quality, or hard-to-sample)

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Take M samples from distribution q(x), turn into N samples from (unnormalized) distribution $\hat{p}(x)$ Typically $N \ll M$, and the N samples become higher quality (i.e., closer to $\hat{p}(x)$) as $M \to \infty$ If M = 1, equivalent to sampling q(x); if $M = \infty$, equivalent to sampling $\hat{p}(x)$



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 $\int S(x) V(x) dx$

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Cleanly decomposes integrand into pieces that get *evaluated at different frequencies*!

Very valuable if S(x) and V(x) have very different costs

This allows computing N rays per pixel using $M \gg N$ (cheaper) shades

The larger M, the better quality your N samples

e.g.,
$$\hat{p}(x) = S(x)$$

Can apply RIS multiple times; imagine picking $\hat{p}(x) = f_r(x)G(x)L(x)$:

$$\int f_r(x) G(x) L(x) V(x) dx \approx \frac{1}{N} \sum \left[V(x_i) \frac{1}{M} \sum \frac{1}{$$

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- Still a legitimately hard integral, evaluated with Monte Carlo
 - Perhaps apply RIS again, to get a good p(x)?

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Let's use a second target function p(x) = G(x)L(x):

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 $\frac{f_r(x_j) G(x_j) L(x_j)}{p(x_i)}$

 $\frac{(x_j) L(x_j)}{L(x_i)} \frac{1}{K} \sum \frac{G(x_k) L(x_k)}{q(x_k)} \|$

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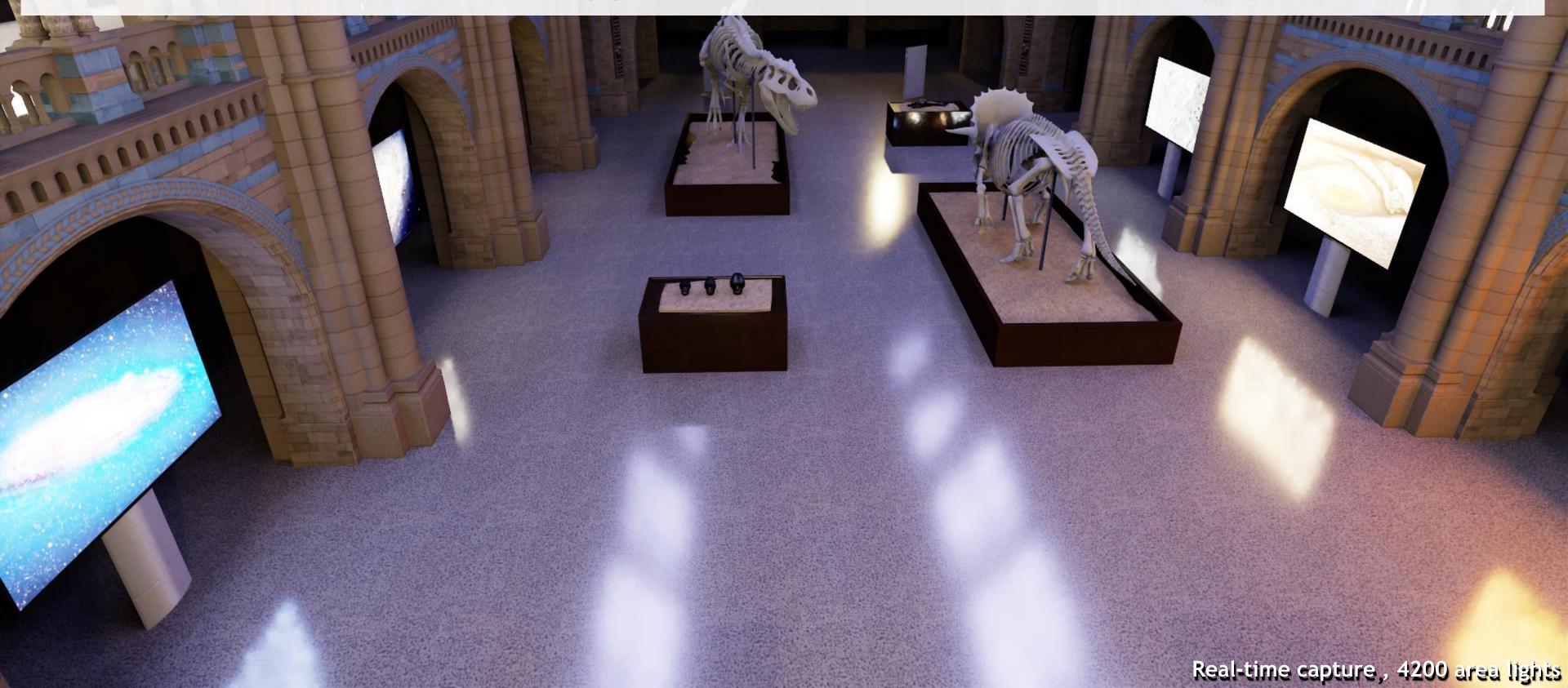
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And now, it's pretty easy to sample $q(x) \sim L(x)$, which allows further cancellation

Able to split numerical integration so *each term* evaluated with *different sampling rate*!

 $\frac{f_r(x_j) G(x_j) L(x_j)}{p(x_i)}$

10000000000000000



Converts M cheap samples into N of better quality

Allows sampling from (nearly) arbitrary functions in an unbiased way

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As $M \rightarrow \infty$, you approach ideal sampling of your target distribution

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Apply RIS in multiple stages

Lots of flexibility for designing algorithms

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As $M \to \infty$, you approach ideal sampling of your target distribution

Apply RIS in multiple stages

Lots of flexibility for designing algorithms

Decouple computational frequencies

Use cheap-to-compute terms to improve placement of expensive operations



TAKING $M \to \infty$

For RIS, you want large pools of candidate samples

What if we target M = 10,000 candidates to pick N = 1 sample...

TAKING $M \to \infty$

For RIS, you want large pools of candidate samples

What if we target M = 10,000 candidates to pick N = 1 sample...

Do you need to keep all 10,000 candidates resident in memory?

If so... limits increases to M

Most people today keep candidates resident

Compute discrete CDF, invert to draw samples

TAKING $M \to \infty$

For RIS, you want large pools of candidate samples

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Compute discrete CDF, invert to draw samples

Why keep 10,000 in memory if returning only one?

Why not discard incrementally?

Keep just N candidates in memory at a given time

WEIGHTED RESERVOIR SAMPLING

Do yourself a favor; learn this algorithm and keep it near the top of your toolbox

Well known algorithm from early 1980s

Data often stored on reel-to-reel tape

Big pain if rewind needed for algorithm's 2nd pass over data



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Streaming selection of arbitrary weighted samples

Constant memory, one pass over data, size need not be known



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Streaming selection of arbitrary weighted samples

Constant memory, one pass over data, size need not be known

Easy proof by induction

Multiple people have reinvented this wheel

But go read up on 40 years of theory



Always pick first sample encountered with weight > 0

Sample stream



Discard old, choose new sample with probability w_{purple} / (w_{purple} + w_{green})

Sample stream



Choose new sample with probability w_{orange} / (w_{orange} + w_{dotted})

Sample stream

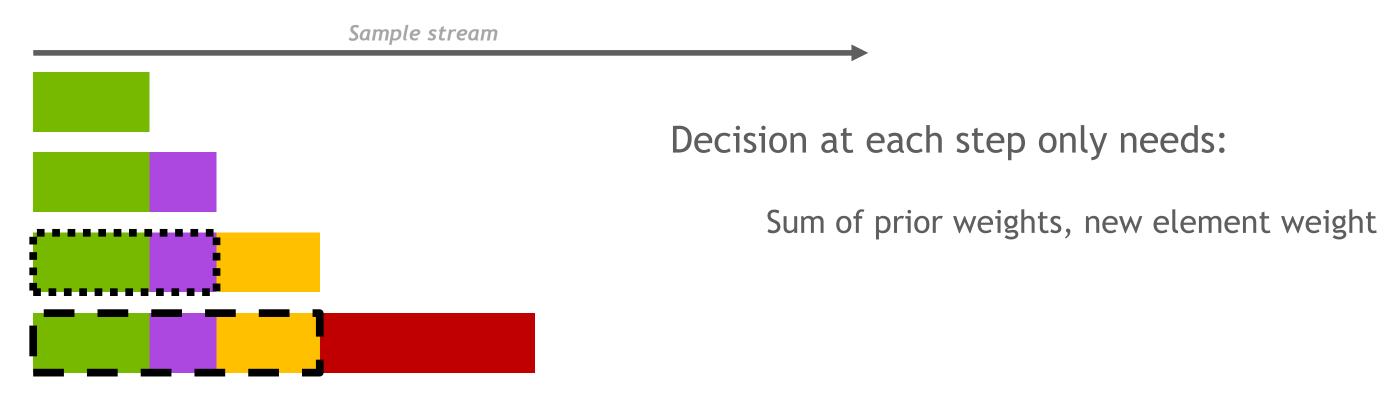


Choose new sample with probability $w_{red} / (w_{red} + w_{dashed})$



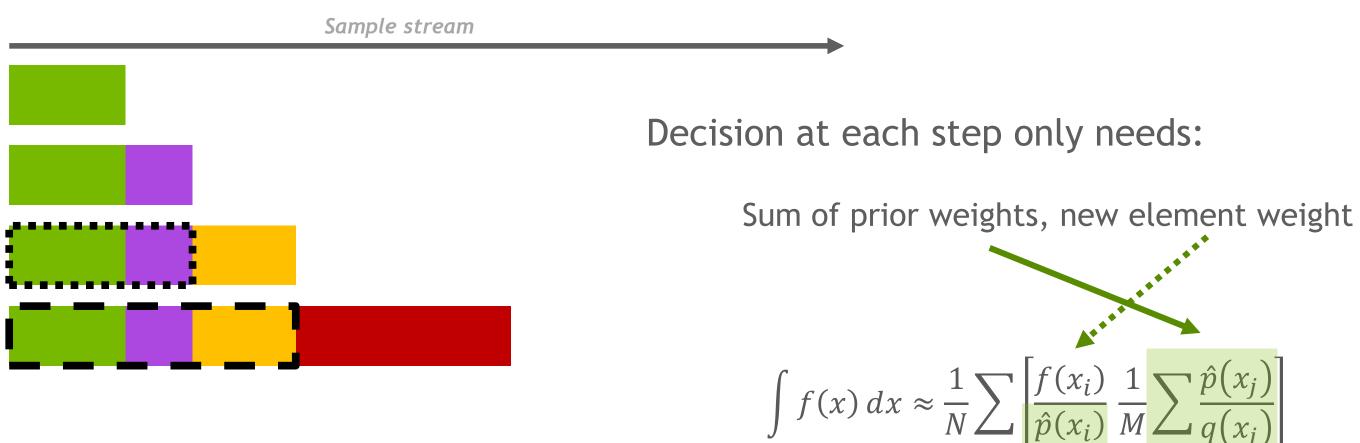


Whenever stream stops, just output current selection as final answer





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Memory O(N), and for real-time this is generally a small constant

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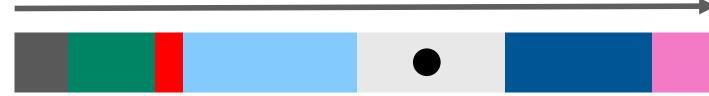
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But, weighted reservoir sampling provides another benefit

Can combine two independent streams of samples

Without reprocessing individual samples!

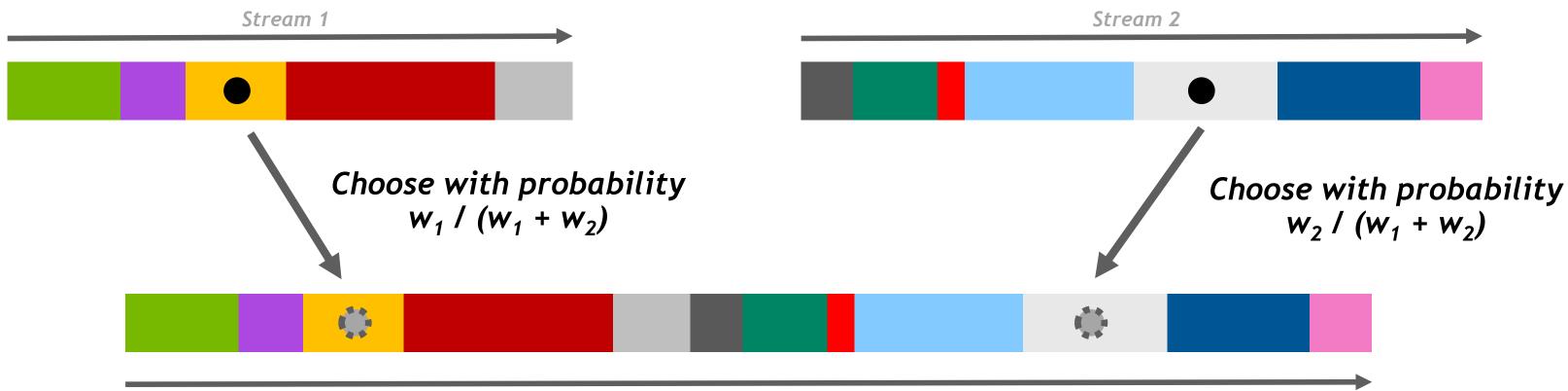




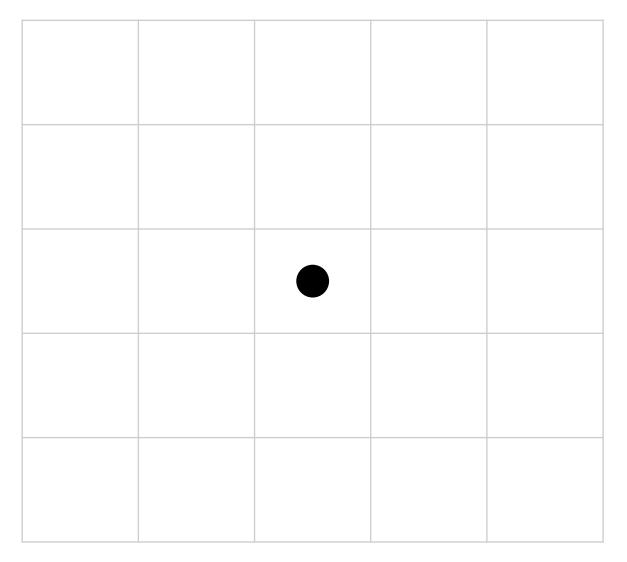
Stream 2

Can combine two independent streams of samples

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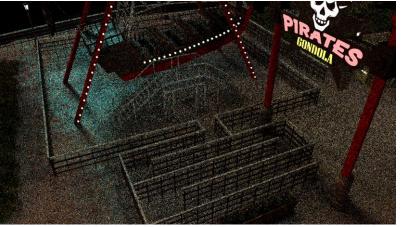


Combined Stream



At each pixel, say we select 1 light from 32 random samples

Using RIS and weighted reservoir sampling



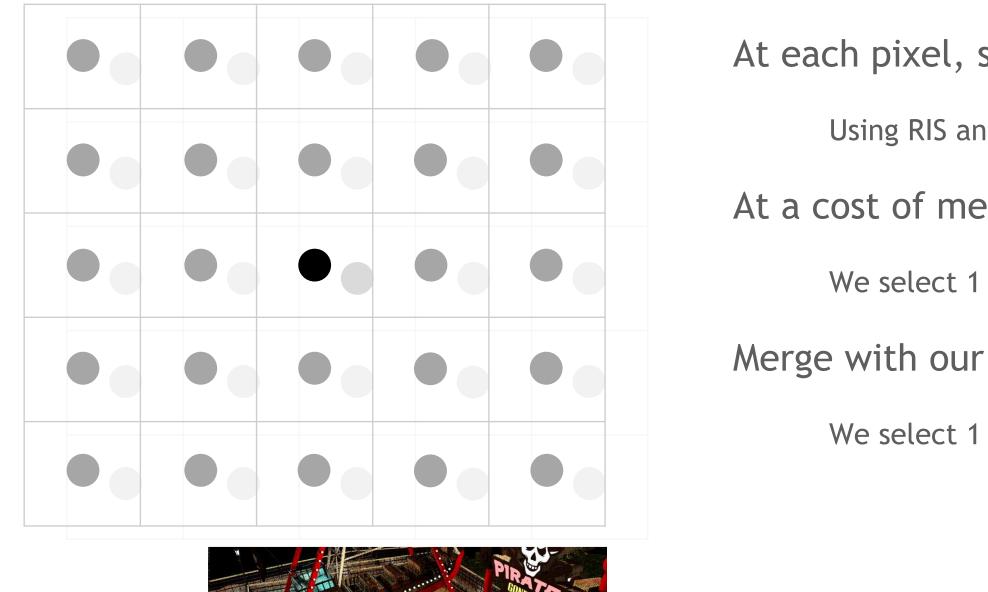


Using RIS and weighted reservoir sampling

At a cost of merging these 25 reservoirs

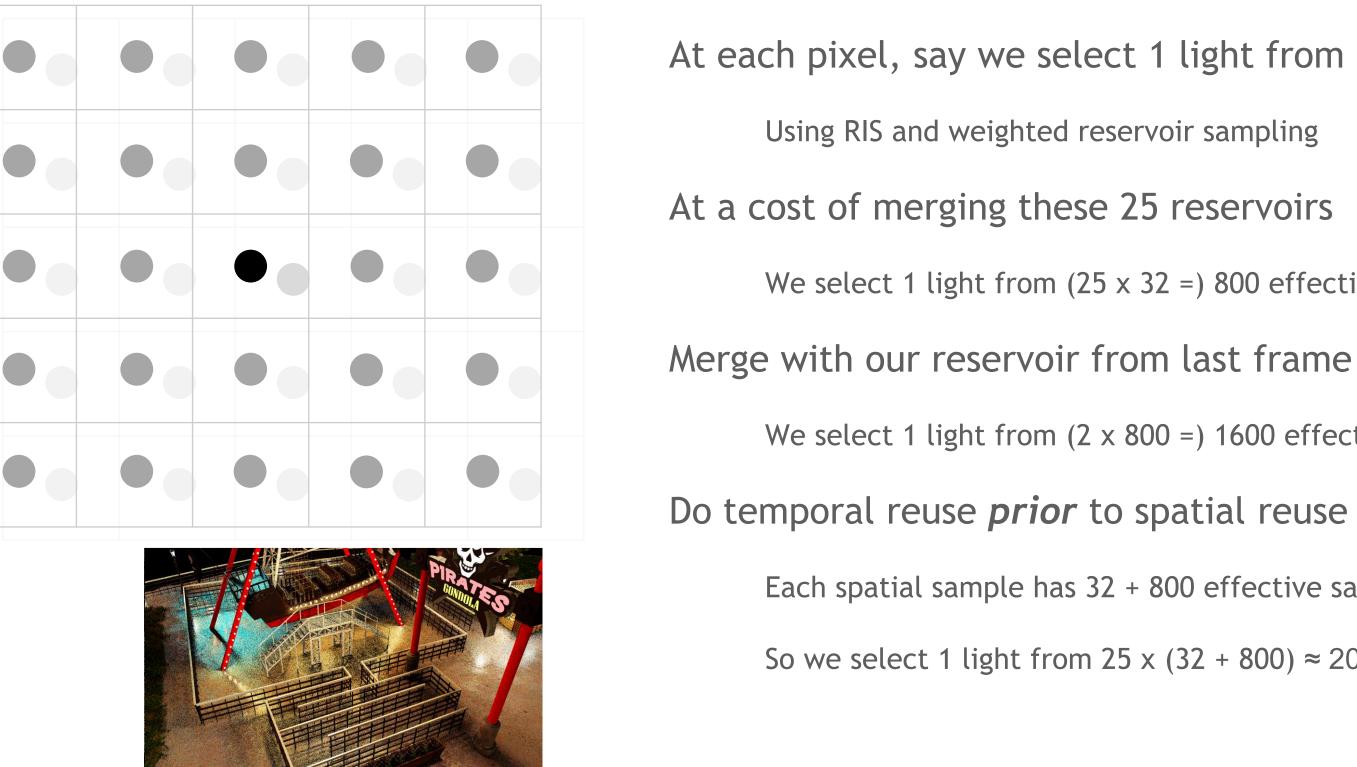
- At each pixel, say we select 1 light from 32 random samples

 - We select 1 light from $(25 \times 32 =) 800$ effective samples



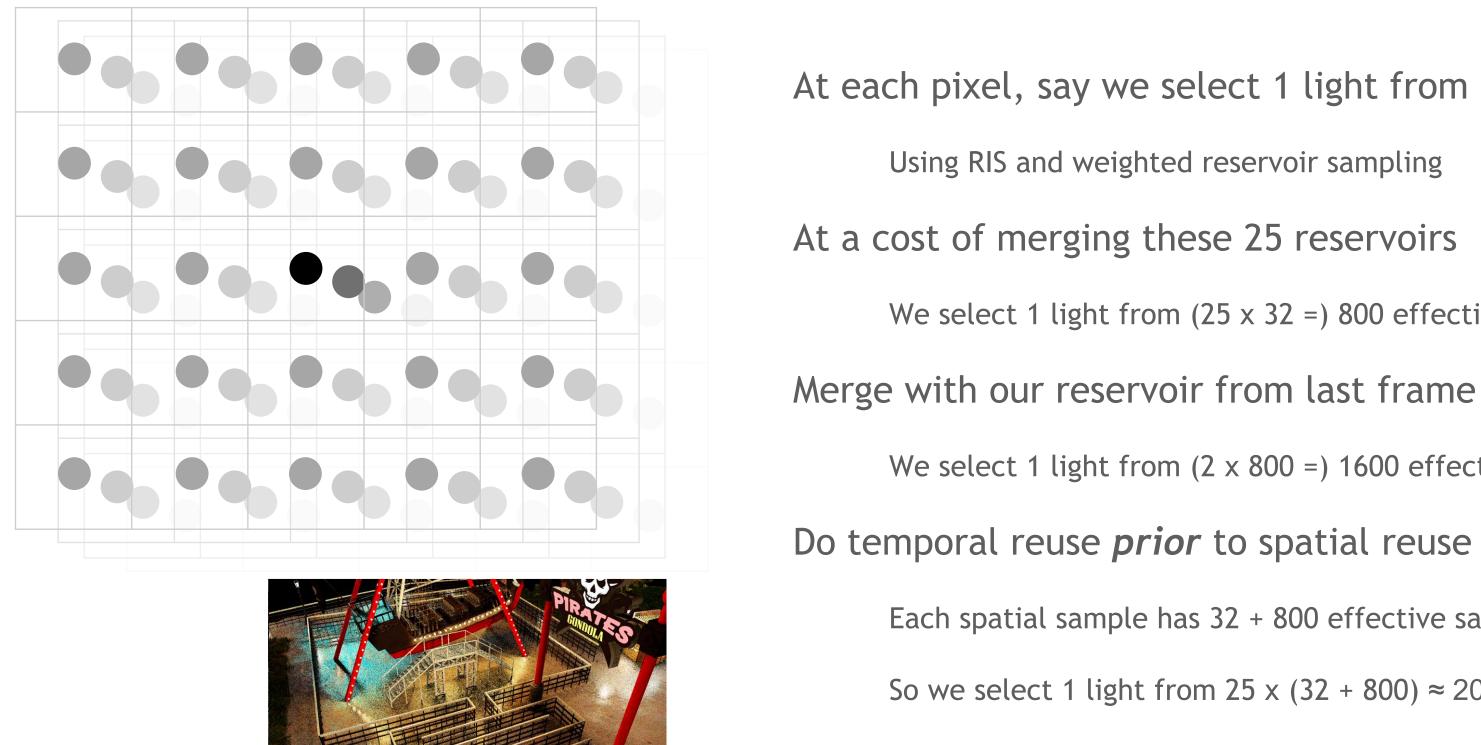


- At each pixel, say we select 1 light from 32 random samples
 - Using RIS and weighted reservoir sampling
- At a cost of merging these 25 reservoirs
 - We select 1 light from $(25 \times 32 =) 800$ effective samples
- Merge with our reservoir from last frame
 - We select 1 light from $(2 \times 800 =)$ 1600 effective samples



- At each pixel, say we select 1 light from 32 random samples

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 - Each spatial sample has 32 + 800 effective samples
 - So we select 1 light from 25 x (32 + 800) \approx 20,000 effective samples



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- Reuse from a frame that reuses it's prior frame...

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What is your target function $\hat{p}(x)$ at each step?

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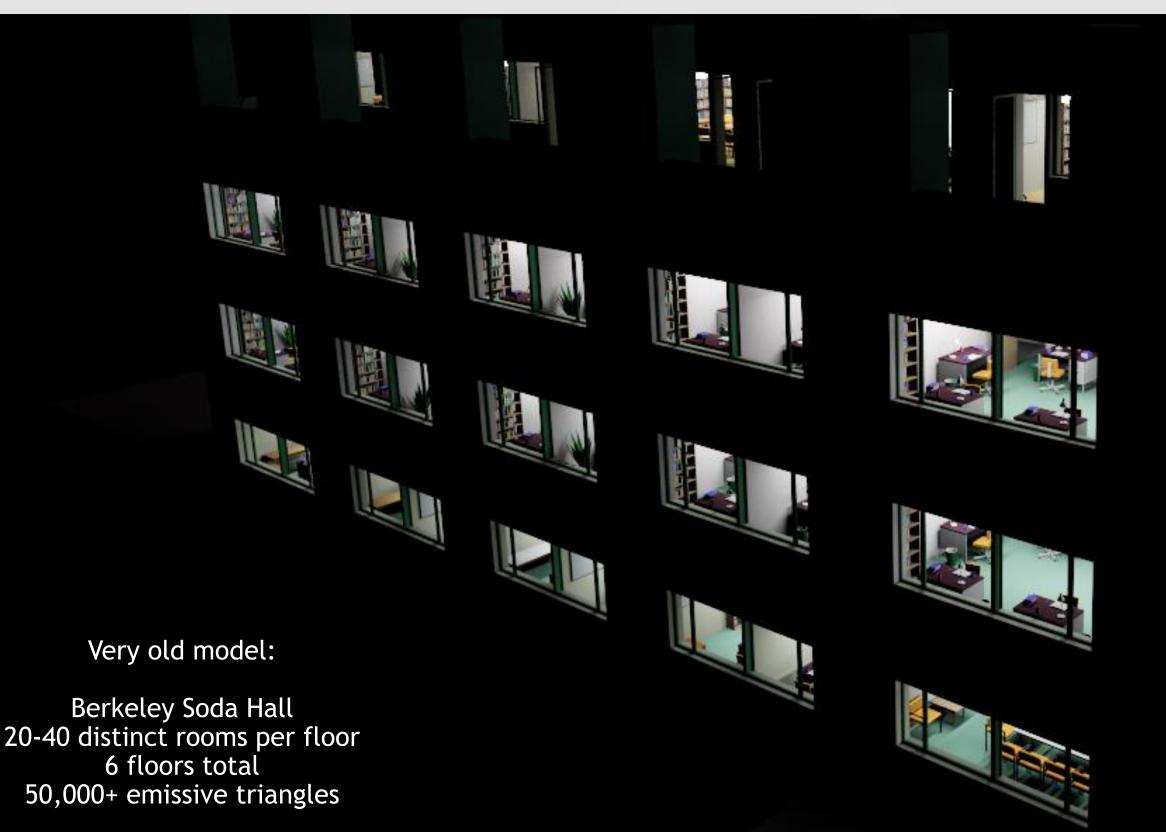
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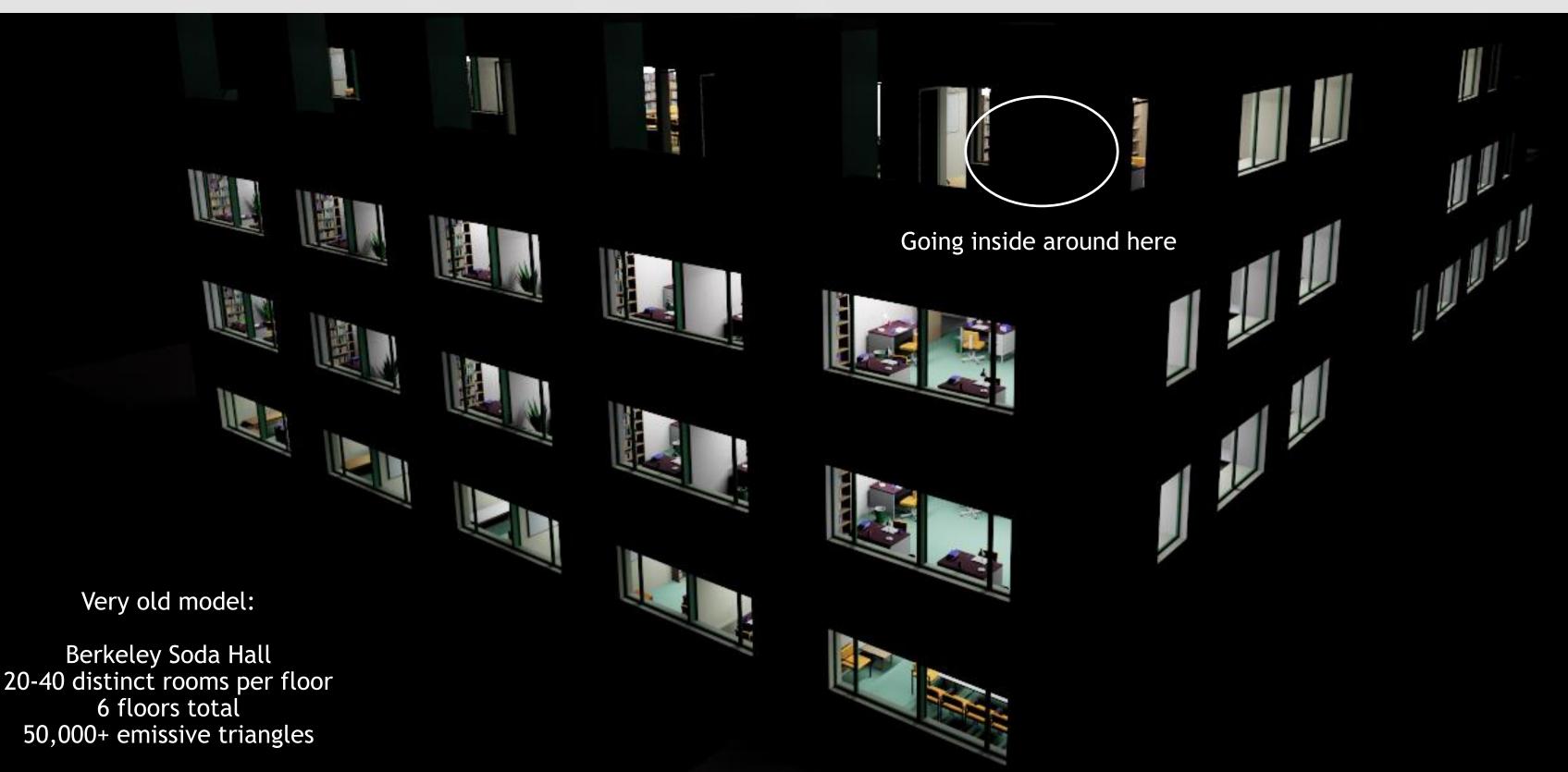
PDFs from neighbor pixels can be quite different; how does this affect sampling quality?

EXPLORING THE DESIGN SPACE: VISIBILITY Visibility one of the most important, most expensive, most ignored aspects of rendering





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Considering all lights in scene, without visibility



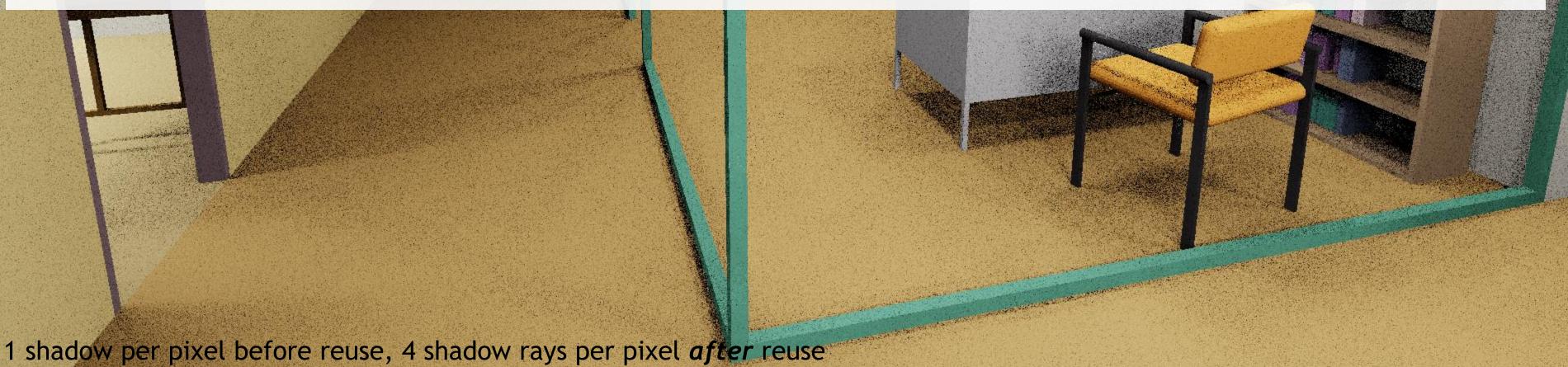






Reusing statistics via RIS still allows varying computation based on signal frequencies!

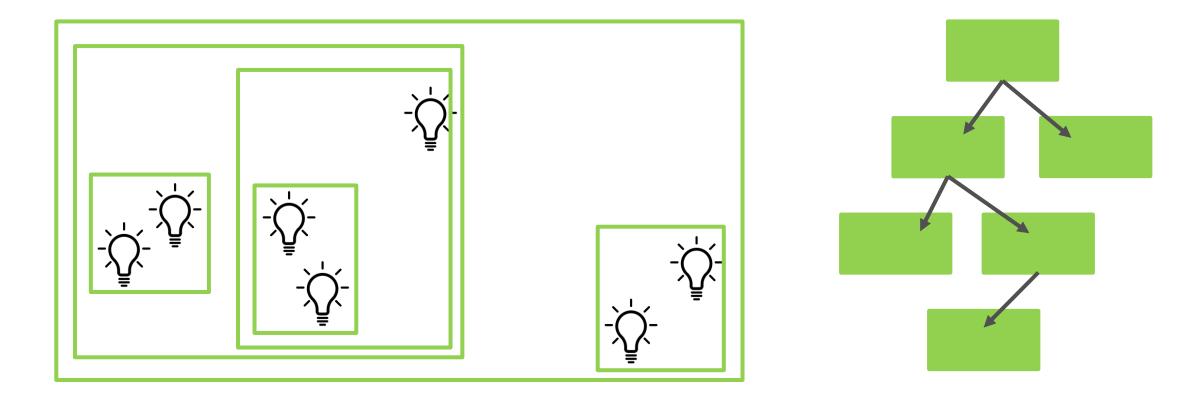
Shadow rays before reuse: "global" shadow rays, give benefits of a light PVS Shadow rays after reuse: "local" shadow rays, give high frequency contact details



ANOTHER WAY TO ABSTRACT THE PROBLEM

We need to accelerate certain sampling processes; how?

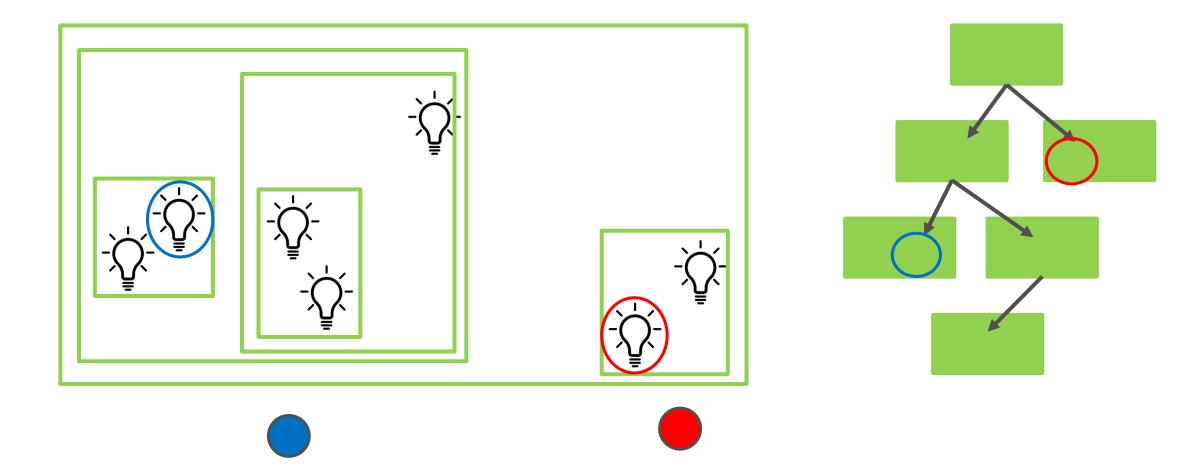
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Frequently some tree

Deterministic build / update

ANOTHER WAY TO ABSTRACT THE PROBLEM We need to accelerate certain sampling processes; how?



Blue pixel more likely to pick from left, red pixel more from the right

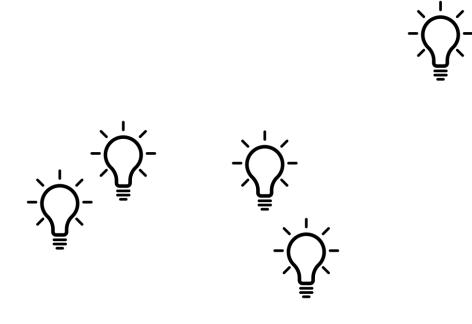
Traverse tree randomly, proportional to (likely) contribution from each child node

Frequently some tree

Deterministic build / update

Traversal is randomized

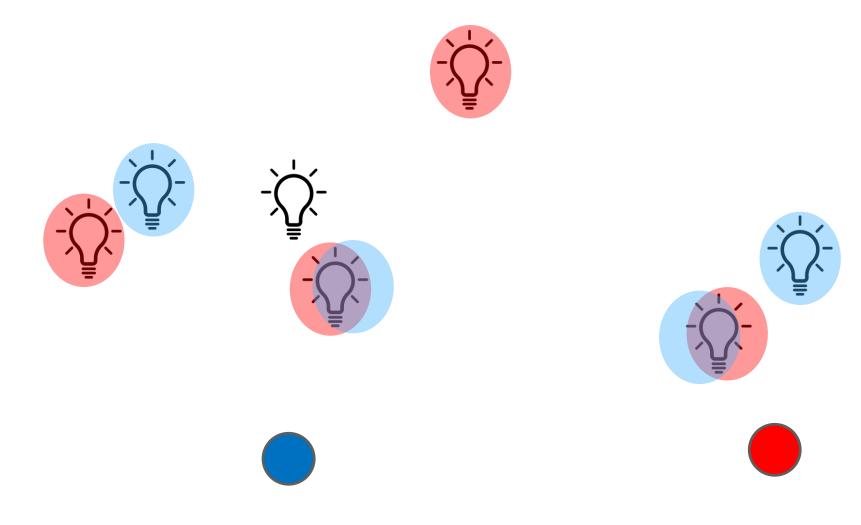
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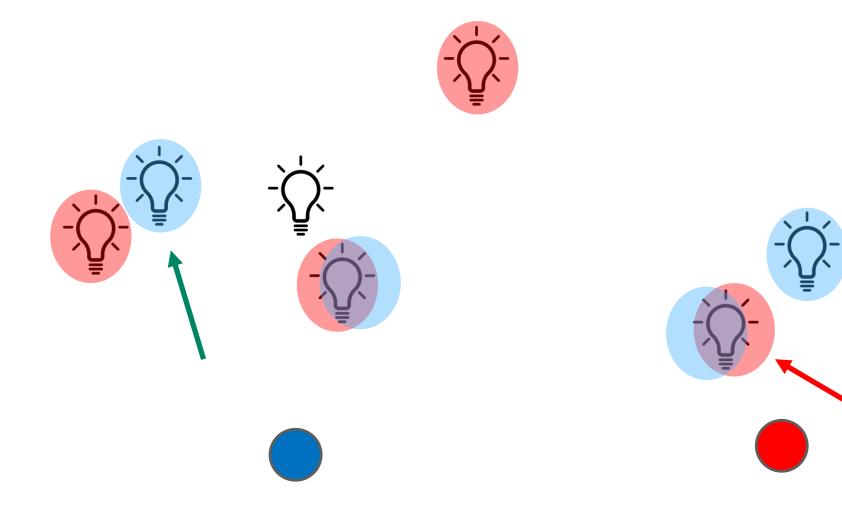
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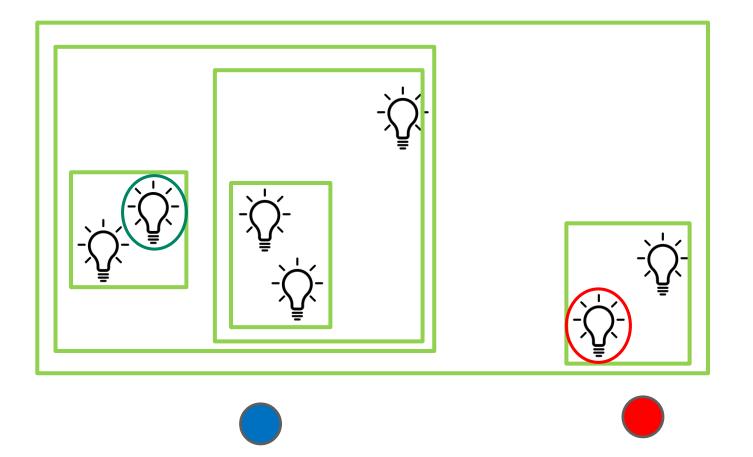
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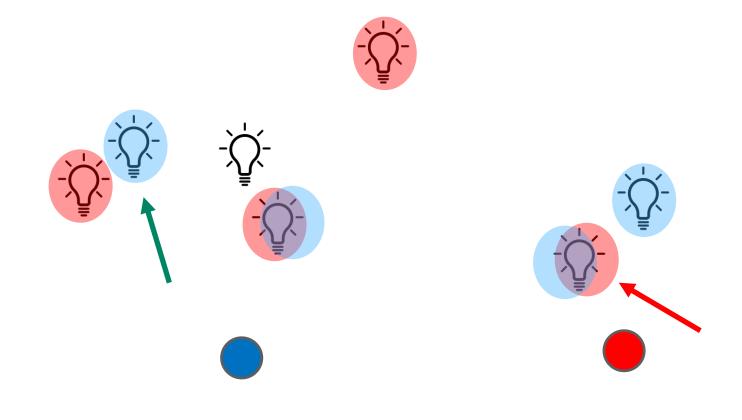
Evaluate likelihood of each candidate

Select one

Proportional to its likelihood

COMPARISON





Rebuild structure for dynamic lights, O(n log n) Random memory reads (stochastic traversal) Dependent memory reads (parent \rightarrow child nodes) Variable cost / divergence (non balanced tree)

No upfront costs

- Random memory reads (candidate selection) Independent memory (do candidates in parallel) Fixed cost (set candidate count; may be larger)

INTERESTING TAKEAWAYS Both relying on randomization

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Both an example of a <u>randomized algorithm</u>

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Different classes of polynomial-time algorithms, with and w/o randomness

Unclear if classes are identical

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Seems important; randomized algorithms you use:

Quicksort, Monte Carlo integration, most light sampling acceleration structures, neural nets

Resampled importance sampling

A form of "sampling importance resampling"

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Also, interesting properties of weighted reservoir sampling Independent v.s. dependent sampling Alternate form using randomized exponentiated weights

Need to build it

(costly)

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Need to maintain it

(costly)

(costly)

Need to build it Need to maintain it Even parts unused this frame

(costly)

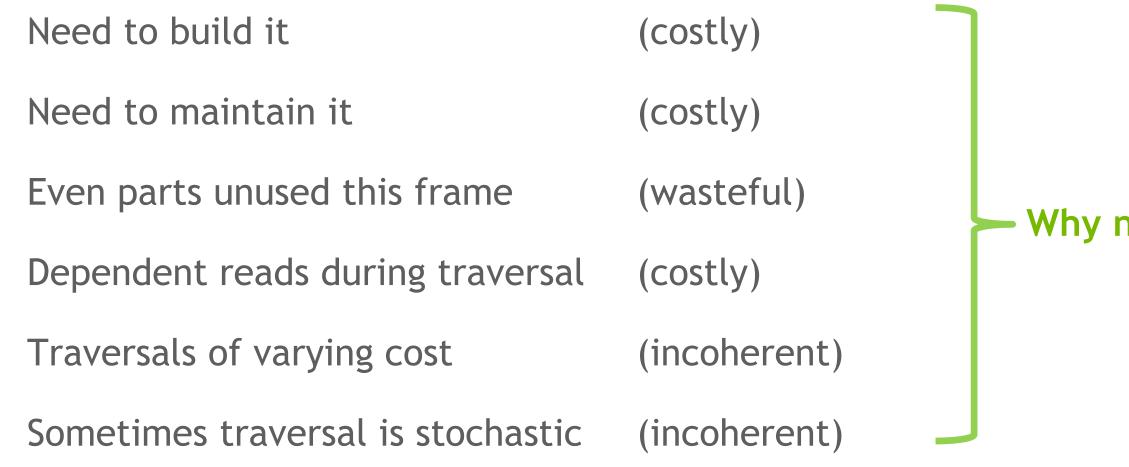
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- Why not use a "randomized" data structure?

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Even parts unused this fr	rame (wasteful)	- Why n
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Instead, a stochastic build with a deterministic traversal

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nore an ideology than a concrete idea

But iterative RIS starts to resemble this

Our goal is to minimize the light tree construction and light sample selection times. The choices we make for achieving this goal, however, may adversely affect the quality of the tree and the light sample distribution. Yet, this reduction in sampling quality can be offset by using more light samples. Thus, our ultimate goal is

Stochastic reuse: Builds tree so loosely it's not recognizable; samples are cheap

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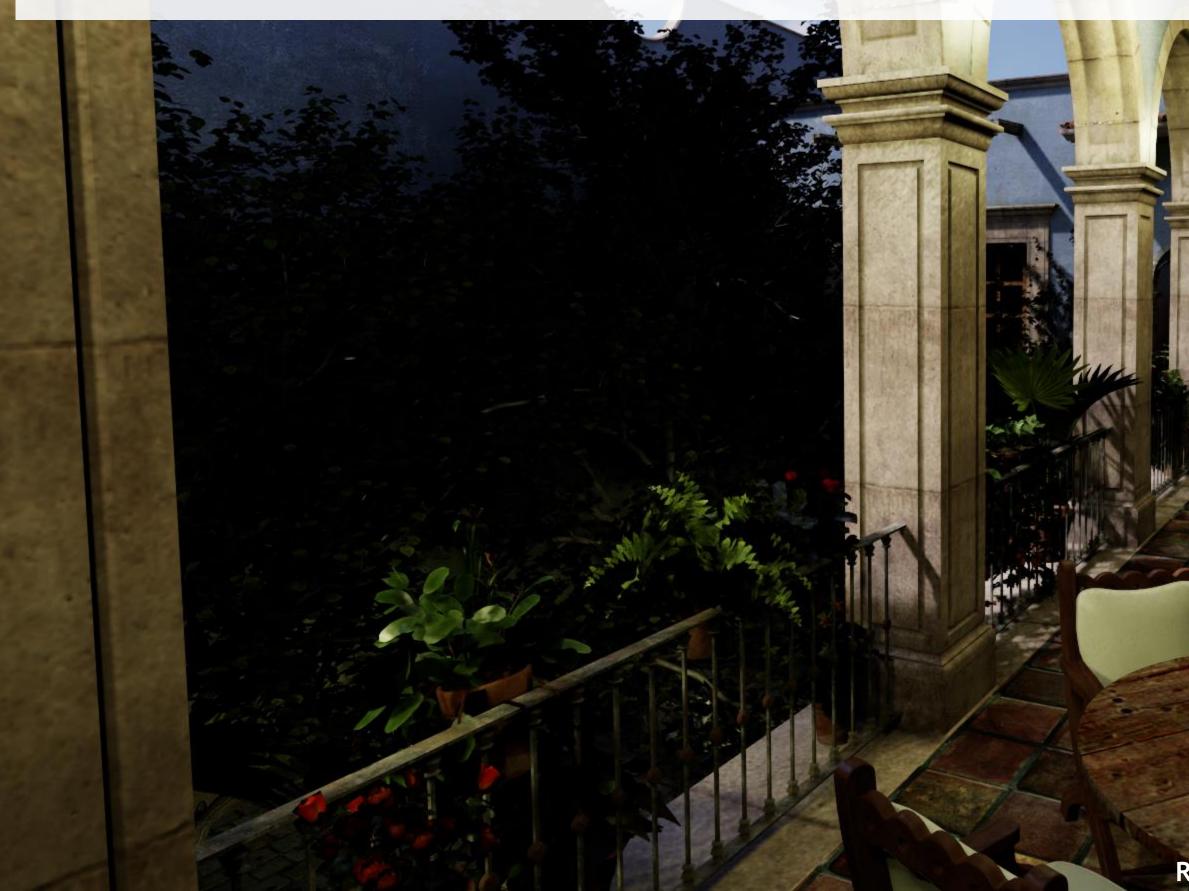
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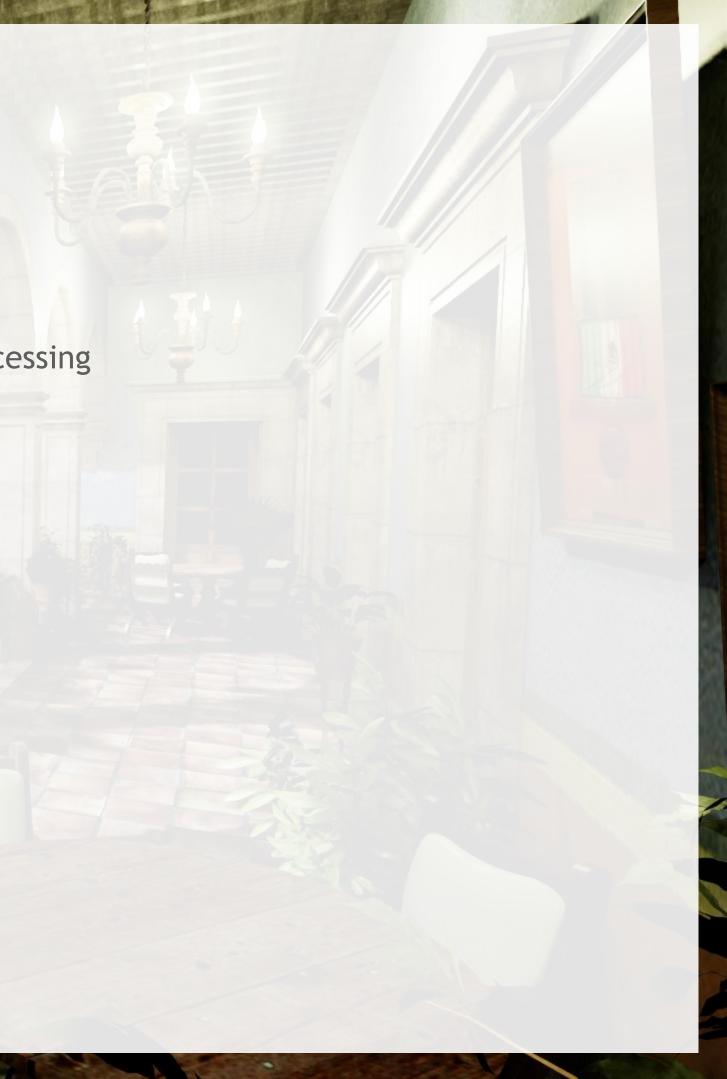
But, it (effectively) uses 100,000+ samples per pixel



Real-time capture, 10,400 area lights + environment map

Real-time ray tracing is here today

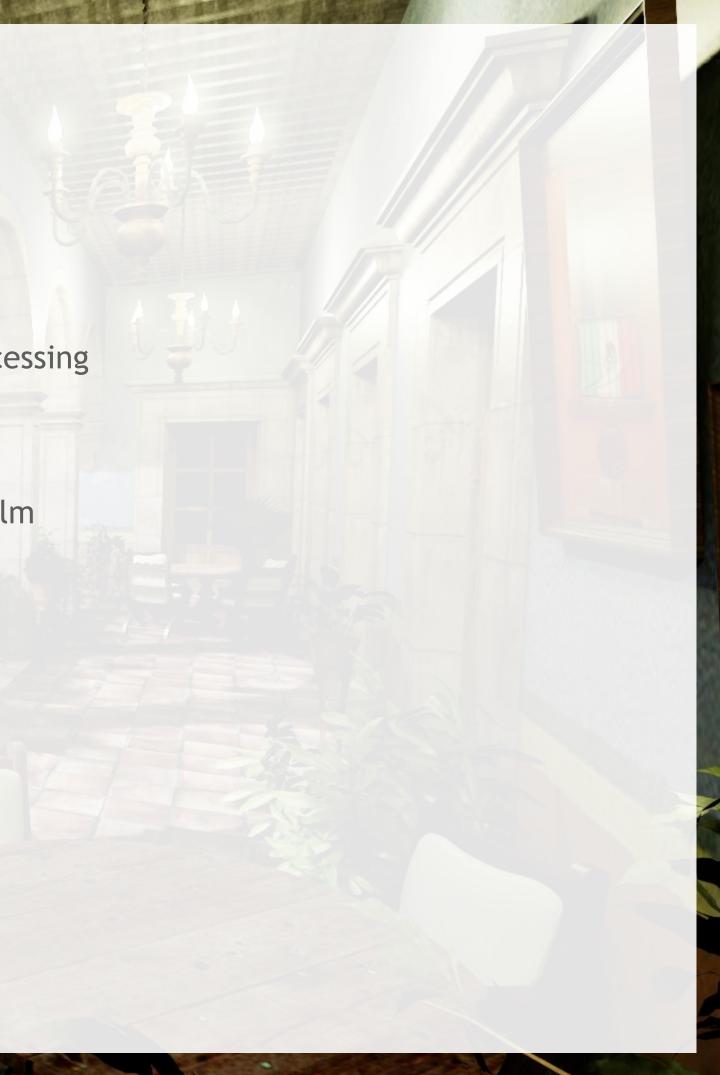
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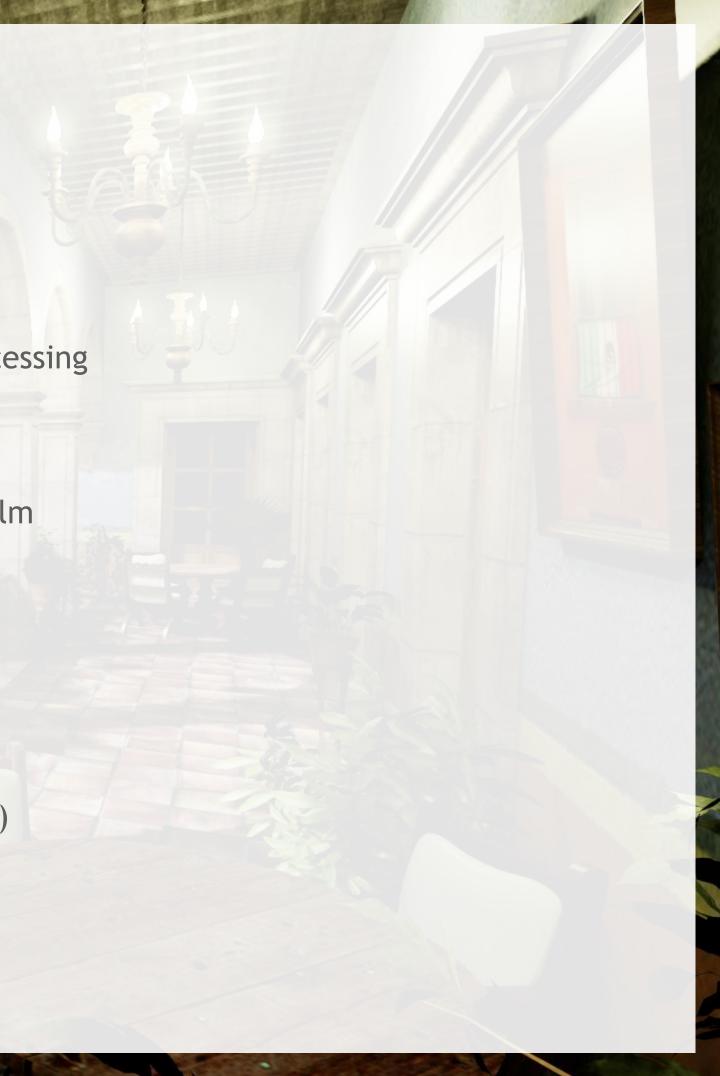
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Rethink complex data structures

Consider streaming statistics and PDFs (rather than triangles and rays)



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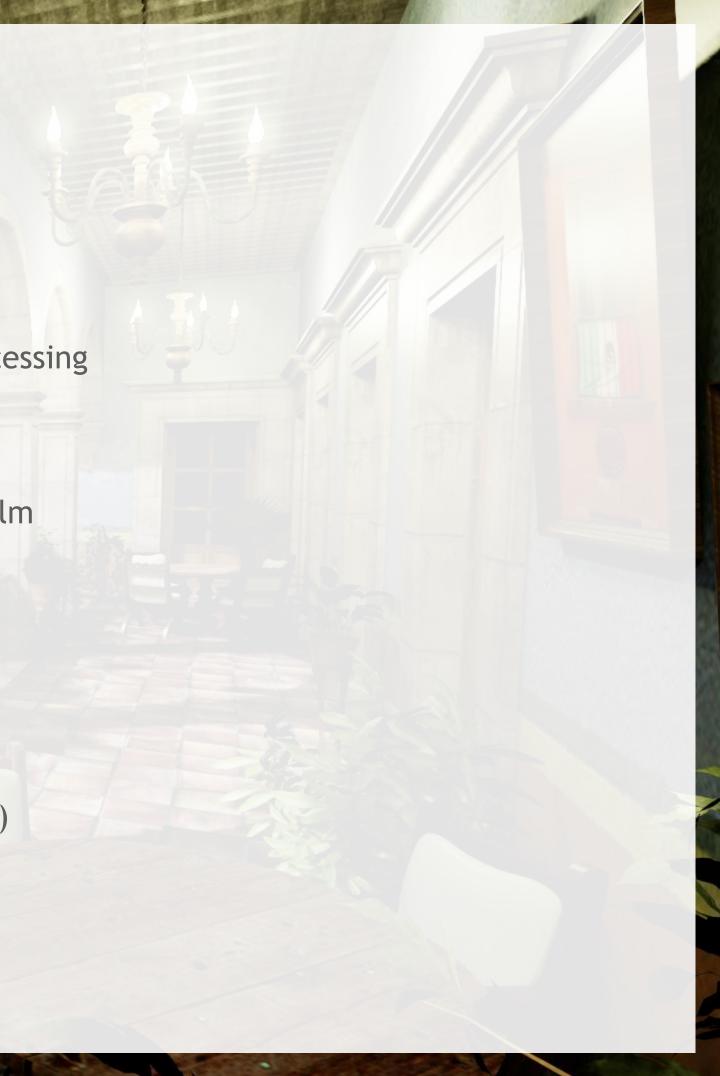
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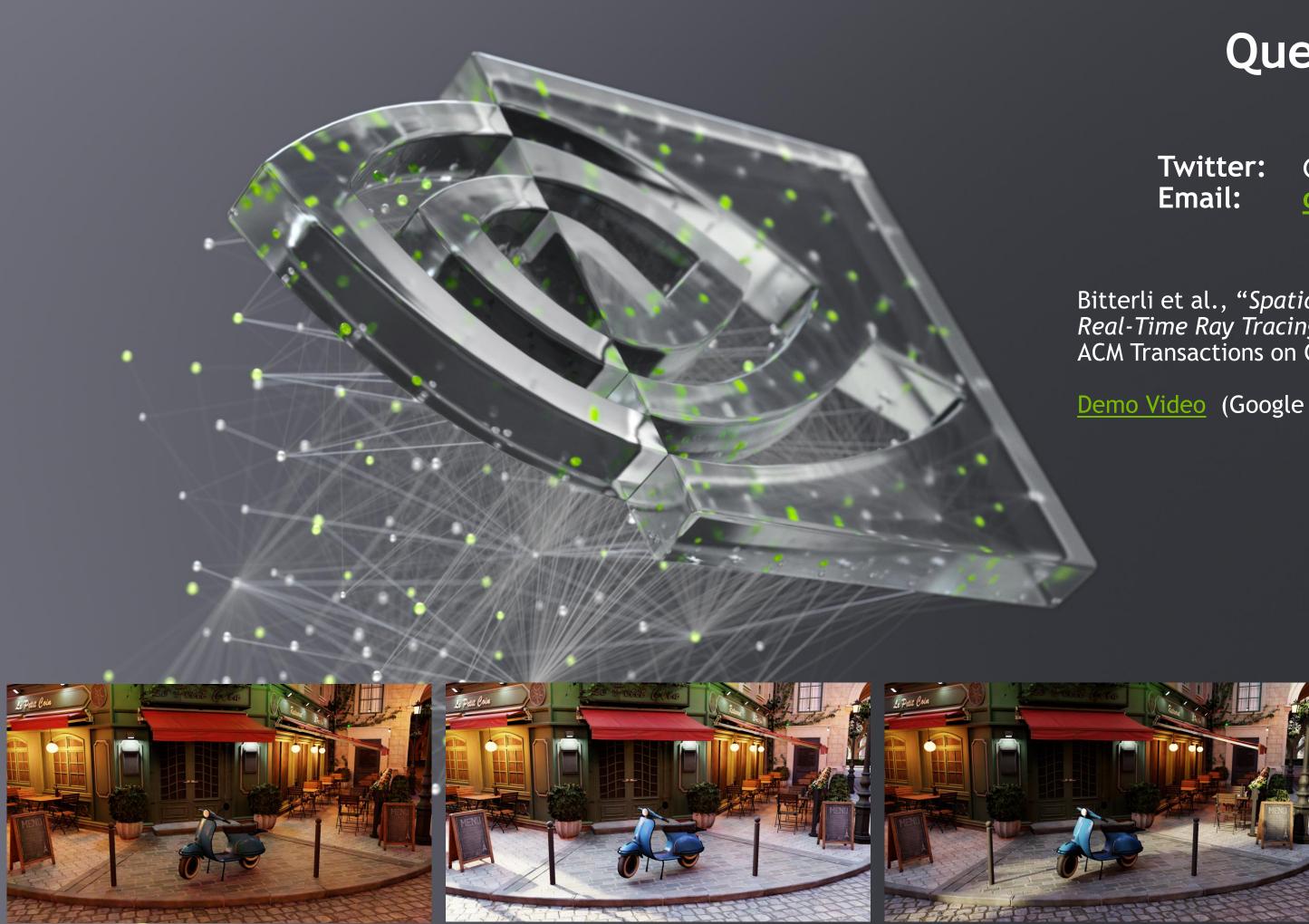
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Likely other ways to reframe the problem

... and people are beating down the doors to try them out







Twitter: @_cwyman_ Email: <u>cwyman@nvidia.com</u>

Bitterli et al., "Spatiotemporal Reservoir Resampling for Real-Time Ray Tracing with Dynamic Direct Lighting," ACM Transactions on Graphics 39(4), Article 148

<u>Demo Video</u> (Google for "NVIDIA ReSTIR YouTube")

